Large-scale anomalies in WMAP data Deviations from isotropy

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Multipole alignments

- Techniques
- Results
- Steerable wavelet anisotropy test
 - Method
 - Results
- Over a symmetry North-south power asymmetry



5 New physics?

- Models
- Corrections
- Problems



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Alignments Steerable wavelets Power asymmetry Cold spot Bianchi

Techniques Results

Multipole alignments

• Decompose CMB into spherical harmonics

$$f(\omega) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} a_{\ell m} Y_{\ell m}(\omega) = \sum_{\ell=0}^{\infty} f_{\ell}(\omega)$$

- Associate preferred directions with each multipole representation $f_{\ell}(\omega)$:
 - Maximum angular momentum dispersion (de Oliveira-Costa et al. 2003)
 - Multipole vectors (Copi et al. 2004)
 - Multipole invariants and frames (Land & Magueijo 2005)



Figure: Illustration of random spherical function and corresponding multipole directions (Dennis 2005)

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Techniques Results

Multipole alignments

• Peculiar planarity and alignment of quadrapole and octopole (de Oliveira-Costa et al. 2003; Copi et al. 2004; etc.) (and also between some other low *l*'s)



(a) Quadrapole ($\ell = 2$)

(b) Octopole ($\ell = 3$)

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Figure: $f_{\ell}(\omega)$ multipole maps

- Some works claim that planar shape is not statistically significant (e.g. Slosar & Seljak 2005; Land & Magueijo 2005) but consensus is that alignment is peculiar (using range of tests)
- Infamously dubbed the Axis of Evil (AoE)



• Various works claim close alignment with ecliptic and/or dipole (e.g. Copi et al. 2006)



Figure: Quadrapole and octopole alignments with ecliptic and dipole

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Alignments Steerable wavelets Power asymmetry Cold spot Bianchi Method Results Steerable wavelets on the sphere

 Steerable wavelets may be expressed as a linear combination of a finite number of basis wavelets



Figure: First derivative of Gaussian on the sphere (Wiaux et al. 2005a)

• Thus wavelet coefficients for any orientation may be derived from coefficients computed for a small number of basis orientations

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Method Results

Steerable wavelet anisotropy test: Method

- Test methodology (Wiaux et al. 2005b, Vielva et al. 2006)
 - Use steerable wavelets to pick out preferred orientation
 - Increment votes for all points on great circle
 - Construct map giving probability a given pixel is seen by local CMB features



Figure: Illustration of steerable wavelet anisotropy test

Analysis run on WMAP data using second derivative of Gaussian

Steerable wavelets anisotropy test: Results

- Anisotropy map shows deviations from anisotropy relative to Monte Carlo simulations
- Pick out great circle, with pole very close to dipole



Figure: Steerable wavelet anisotropy results

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North-south power asymmetry

- ML estimate of local angular power spectrum on small patches (Eriksen et al. 2004)
- Amplitude of disks in the northern Galactic hemisphere generally lower than in simulated maps; amplitude of disks in the southern Galactic hemisphere generally higher than in simulated maps



Figure: Power spectrum comparison

North-south power asymmetry

- Colour of disks indicates power ratio relative to overall power
- Axis of maximum asymmetry found to be close to ecliptic



Figure: Local power spectrum analysis

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Cold spot

 Deviations from Gaussianity detected in kurtosis of spherical Mexican hat wavelet (SMHW) (Vielva et al. 2004)



Figure: SMHW kurtosis

- Large non-Gaussian cold spot detected
- Various test statistics indicate extremely large and cold spot unlikely at >99% level (Cruz et al. 2004, 2006a, 2006b)

Cold spot

- Morphology approximately circular
- Excluding the spot the data are consistent with Gaussianity (using the SMHW kurtosis test)
- Not systematics, not foregrounds
- Origin?
 - Topological defect (texture)
 - Rees-Sciama effect
 - Others?



(a) SMHW coefficients



(b) $22^\circ \times 22^\circ$ patch

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Figure: Cold spot

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New physics?

- Non-trivial topologies (de Oliveira-Costa et al. 2003; Cresswell et al. 2005)
- Spontaneous isotropy breaking (Gordon et al. 2005)
- Relic anisotropy due to initial conditions (Gümrükcüglu et al. 2006)
- Bianchi models exhibiting universal shear and rotation (Barrow et al. 1985)
- Other exotic models?

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Bianchi models

- Relaxing assumption of isotropy about each point in universe yields more complicated solutions to Einstein's field equations
- A universal shear and rotation induce characteristic signature in the CMB
- CMB temperature fluctuations derived by Barrow et al. (1985), albeit in the absence of dark energy since it was not considered plausible at the time
- Interest in Bianchi models rekindled recently (will motivate soon)
- Recently, CMB temperature fluctuations derived when incorporating dark energy independently by Jaffe et al. (2006) and Lasenby (to appear)
- Statistically significant template detected in WMAP data (Jaffe et al. 2005)





Bianchi corrections to WMAP

• Use best-fit Bianchi template to 'correct' the WMAP data



Figure: Bianchi correction (Jaffe et al. 2005)

• Remarkably, many of the anomalies discussed previously disappear after the WMAP data is corrected by the best-fit Bianchi component (Jaffe et al. 2005):



• Multipole alignments disappear or are significantly mitigated



Figure: Quadrapole and octopole

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• Significance of any power asymmetry drops from 99.3% to 86.4%



Figure: Power asymmetry

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SMHW kurtosis is essentially compatible with Gaussianity



Figure: SMHW kurtosis

Bianchi corrections to WMAP

- Bianchi template is inconsistent with concordance cosmology
- Bianchi degeneracy tested using MCMC sampling (Bridges et al. 2006)
- Bianchi parameters detached from cosmological ones
- No longer physically motivated
- For more see Michael Bridges' talk at the Cavendish, Tue 17th Oct



Figure: Bianchi template degeneracy (Bridges et al. 2006)

Summary

- Cosmological principle of fundamental importance
- Many anomalies reported in WMAP data violating this principle
- A number of attempts have been made to explain these anomalies (e.g. by foregrounds, systematics, exotic models) but no satisfactory solution is evident
- Motivation to pursue more exotic models that may be able to describe the observed anomalies

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