



Towards Learned Exascale Computational Imaging (LEXCI) for Radio Astronomy

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Image Reconstruction at Scale: Challenges and Collaboration,
University of Cambridge, 2025



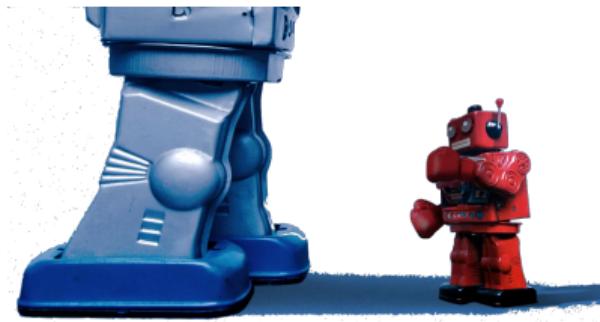
UK Research
and Innovation



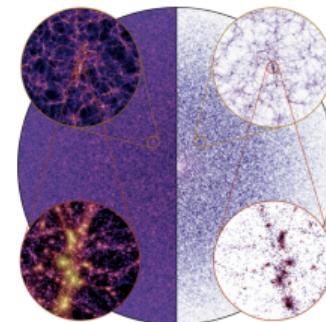
Exascale computational challenges



Big-Data



Big-AI



Big-Sims

⇒ All require **Big-Compute**.

Overview

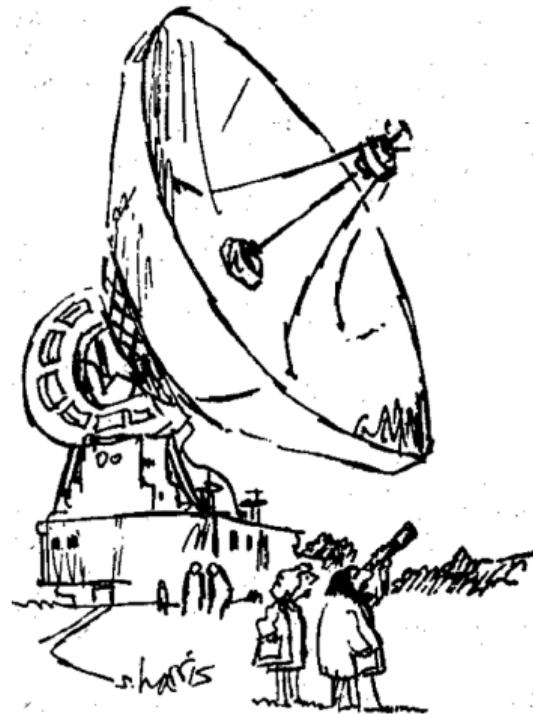
1. SKA Exascale
2. Imaging Strategy
3. Exascale Algorithms
 - Distribution
 - Uncertainty Quantification
 - AI Data-Driven Prior
4. Demonstrations

SKA Exascale





Radio telescopes are big!



"Just checking."

Radio telescopes are big!



Very Large Array (VLA) in New Mexico



Square Kilometre Array (SKA): next-gen radio interferometric telescope



SPDO / Swinburne Astronomy Productions

SKA science goals

Orders of magnitude improvement in sensitivity and resolution.

Unlock broad range of science goals.

Probing
the
cosmic
dawn
⊕

Challenging
Einstein
⊕

Cosmology
and dark
energy
⊕

Exploring
galaxy
evolution
⊕

Our
home
galaxy
⊕

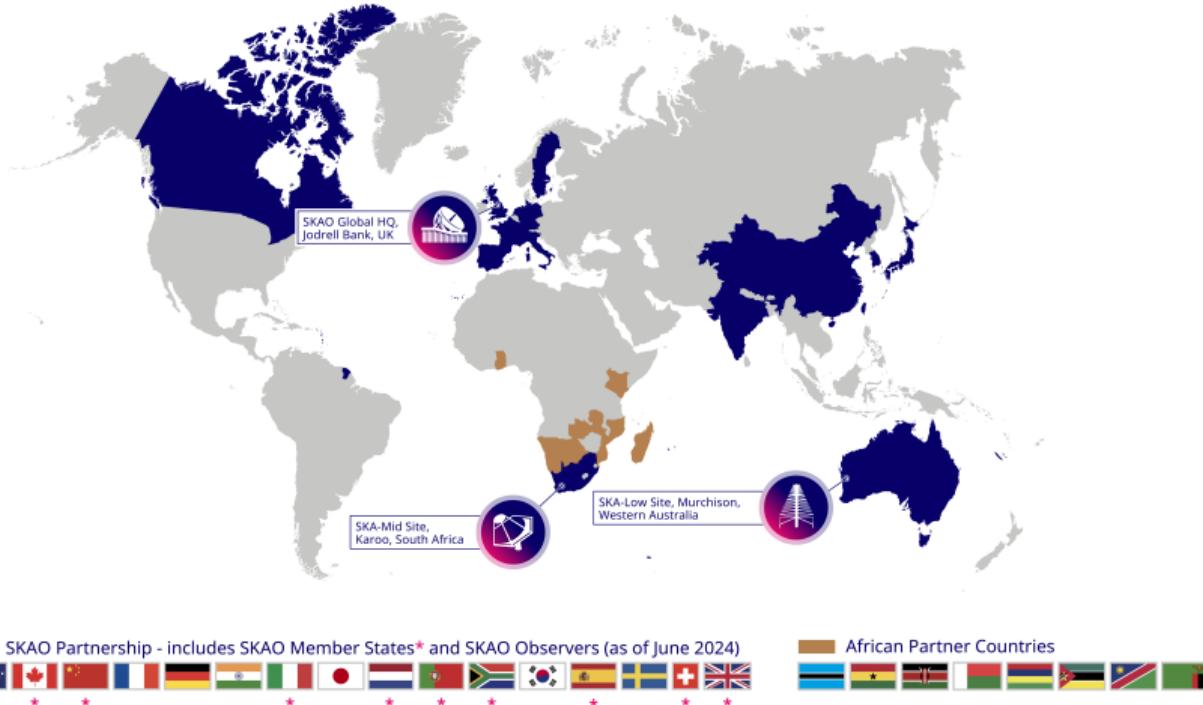
Seeking
the
origins of
life
⊕

Studying
our
nearest
star
⊕

Understanding
cosmic
magnetism
⊕

The
bursting
sky
⊕

SKA partners



SKA sites

SKA-mid – the SKA's mid-frequency instrument

The SKA Observatory (SKAO) is a next-generation radio astronomy facility that will revolutionise our understanding of the Universe. The SKA consists of two instruments, SKA-low and SKA-mid, operating two telescopes on their continents. The two telescopes, named SKA-low and SKA-mid, will be observing the Universe at different frequencies. They are also called interferometers as they each comprise a large number of individual elements working together to form a single large telescope.

Location: South Africa

Frequency range: 350 MHz to 15.4 GHz (with a goal of 24 GHz)

197 dishes (including 62 MeerKAT dishes)

Total collecting area: 33,000m² or 126 tennis courts

Maximum distance between dishes: 150km

Data transfer rate: 8.8 Terabits per second

Image quality of SKA-mid (left) versus the best current facility operating in the same frequency range, the Jansky Very Large Array (JVLA) in the United States (right). SKA-mid's resolution will be 4x better than JVLA.

Compared to the JVLA, the current best similar instrument in the world:

- 4x the resolution
- 5x more sensitive
- 60x the survey speed



www.skatelescope.org      

SKA-low – the SKA's low-frequency instrument

The SKA Observatory (SKAO) is a next-generation radio astronomy facility that will revolutionise our understanding of the Universe. The SKA consists of two instruments, SKA-low and SKA-mid, operating two telescopes on three continents. The two telescopes, named SKA-low and SKA-mid, will be observing the Universe at different frequencies. They are also called interferometers as they each comprise a large number of individual elements working together to form a single large telescope.

Location: Australia

Frequency range: 50 MHz to 350 MHz

131,072 antennas spread across 512 stations

Total collecting area: 0.4km²

Maximum distance between stations: >65km

Data transfer rate: 7.2 Terabits per second

Image quality of SKA-low (left) versus the best current facility operating in the same frequency range, the LOFAR Netherlands (right). SKA-low's resolution will be similar to LOFAR.

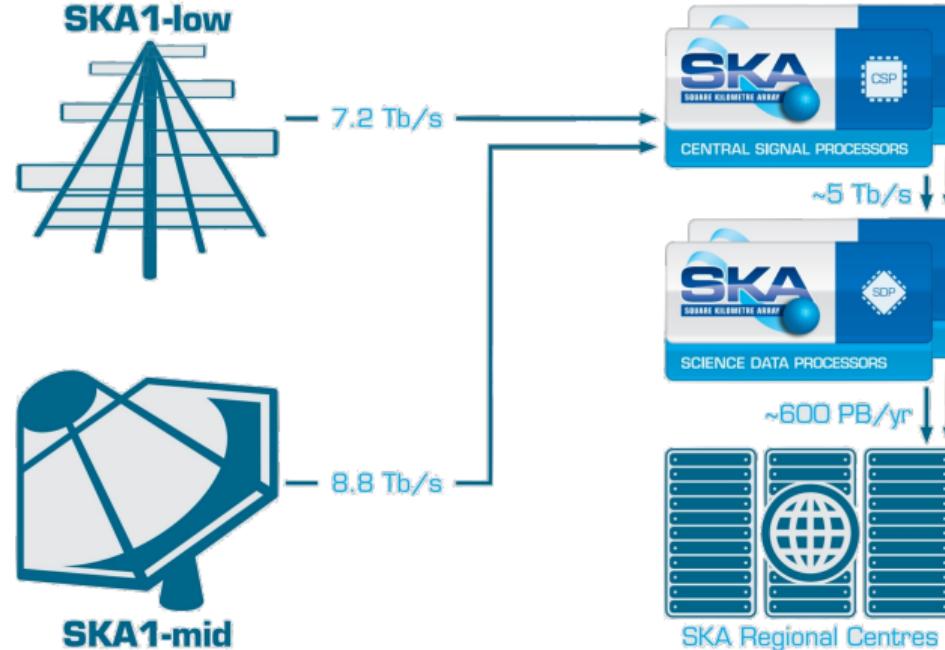
Compared to LOFAR Netherlands, the current best similar instrument in the world:

- 25% better resolution
- 8x more sensitive
- 135x the survey speed



www.skatelescope.org      

SKA data rates



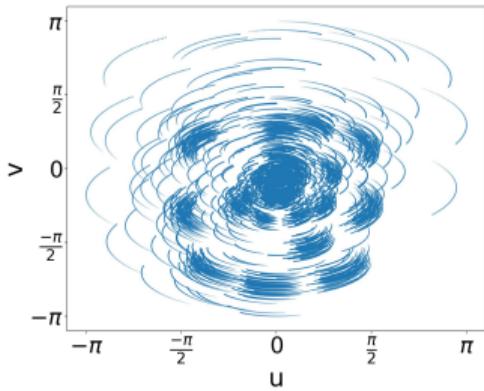
⇒ 8.5 Exabytes over the 15-year lifetime of initial high-priority science programmes
(Scaife 2020).

Imaging Strategy

Radio interferometric telescopes acquire “Fourier” measurements



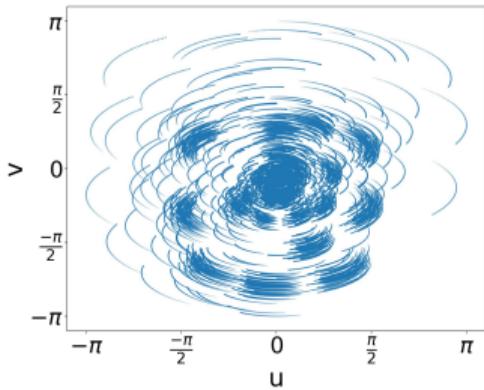
“Fourier”
Measurements
⇒



Radio interferometric telescopes acquire “Fourier” measurements



“Fourier”
Measurements
 \Rightarrow



Interferometric imaging is an **exascale computational inverse imaging problem**.

Radio interferometric inverse problem

Radio interferometric imaging ill-posed inverse problem:

$$y = \Phi(x) + n$$

$$y \xleftarrow{\text{forward model}} x$$

$$y \xrightarrow{\text{inverse inference}} x$$

for data (visibilities) y , telescope model Φ , underlying image x and noise n .

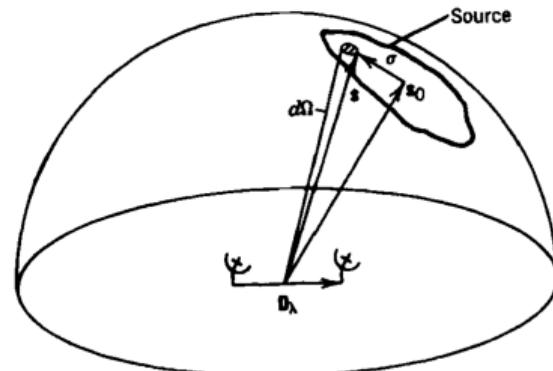
Radio interferometric forward model

Highly realistic wide-field telescope model

(Pratley, Johnston-Hollitt & McEwen 2019; Pratley, Johnston-Hollitt & McEwen 2020).

Forward model, e.g. $\Phi = GCFA$, may incorporate:

- ▷ primary beam A of the telescope;
- ▷ Fourier transform F ;
- ▷ convolutional de-gridding G to interpolate to continuous Fourier coordinates;
- ▷ baseline dependent effects, e.g. varying beam, wide-field effects, captured by GC .



Wide-field scenario.

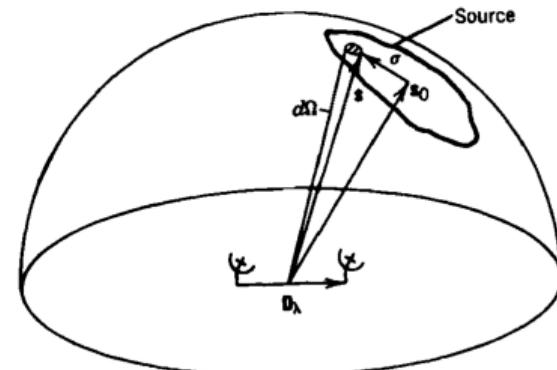
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Wide-field scenario.

Big-Data \Rightarrow Big-Compute

since compute scales as $\mathcal{O}(M)$ for M data measurements.

Statistical framework

Inverse problem is ill-posed so **inject regularising prior information.**

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Bayes Theorem:

$$p(x|y) \propto p(y|x)p(x), \quad \text{i.e. posterior} \propto \text{likelihood} \times \text{prior}$$

Define likelihood (assuming Gaussian noise) and prior:

$$p(y|x) = \mathcal{L}(x) \propto \exp\left(-\|y - \Phi x\|_2^2/(2\sigma^2)\right)$$

likelihood

$$p(x) = \pi(x) \propto \exp(-R(x))$$

prior

Optimisation vs sampling

MAP estimation

MCMC sampling

Optimisation vs sampling

MAP estimation

- ✓ Based on optimisation so **computationally efficient**.

MCMC sampling

- ✗ Based on sampling so **computationally demanding**.

Optimisation vs sampling

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- ✗ No uncertainties (traditionally).

MCMC sampling

- ✗ Based on sampling so **computationally demanding**.
- ✓ **Uncertainties** encoded in posterior.

Optimisation vs sampling

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- ✓ Based on optimisation so **computationally efficient**.
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- ✗ Hand-crafted priors (traditionally).

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Computational imaging strategy

Goals:

- ✓ Computationally efficient (optimisation + distribution).
- ✓ Quantifies uncertainties (for scientific inference).
- ✓ Data-driven AI priors (enhance reconstruction fidelity).

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Solution:

1. Statistical framework: Bayesian inference and MAP estimation.
2. Mathematical theory: probability concentration theorem for log-convex distributions.
3. Constrained AI model: convex AI model with explicit potential.

Solve optimisation problem

Solve optimisation problem (MAP estimation by variation regularisation):

$$\mathbf{x}_{\text{map}} = \arg \max_{\mathbf{x}} [\log p(\mathbf{y} | \mathbf{x})] = \arg \min_{\mathbf{x}} \left[\|\mathbf{y} - \Phi \mathbf{x}\|_2^2 + \lambda R(\mathbf{x}) \right].$$

regulariser

(Also consider constrained formulation.)

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Traditionally, **hand-crafted regularisers** used

(e.g. $R(\mathbf{x}) = \|\Psi^\dagger \mathbf{x}\|_1$ to promote sparsity in some (wavelet) dictionary Ψ).

Instead, adopt **data-driven AI prior** for regulariser (**Small-AI**) trained on simulations
(potentially **Big-Sims**).

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Solve by **highly distributed and parallelised optimisation algorithms**, with **low communication overhead** (Pratley, McEwen *et al.* 2016, Pratley, Johnston-Hollitt & McEwen 2018, 2019, Pratley & McEwen 2019).

Exascale Algorithms

Exascale Algorithms Distribution

Block distribution

Solve resulting convex optimisation problem by **proximal splitting**
(FISTA, ADMM, primal dual).

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Block algorithm to **distribute data and compute** (telescope model):

(Boyd *et al.* 2010; Carrillo, McEwen & Wiaux 2014; Onose *et al.* (inc. McEwen) 2016; Pratley, Johnston-Hollitt & McEwen 2019; Pratley, McEwen *et al.* 2019; Pratley, Johnston-Hollitt & McEwen 2020)

$$\mathbf{y} = \begin{bmatrix} y_1 \\ \vdots \\ y_{n_d} \end{bmatrix}, \quad \boldsymbol{\Phi} = \begin{bmatrix} \boldsymbol{\Phi}_1 \\ \vdots \\ \boldsymbol{\Phi}_{n_d} \end{bmatrix} = \begin{bmatrix} \mathbf{G}_1 \mathbf{M}_1 \\ \vdots \\ \mathbf{G}_{n_d} \mathbf{M}_{n_d} \end{bmatrix} \mathbf{FZ}.$$

Block distribution

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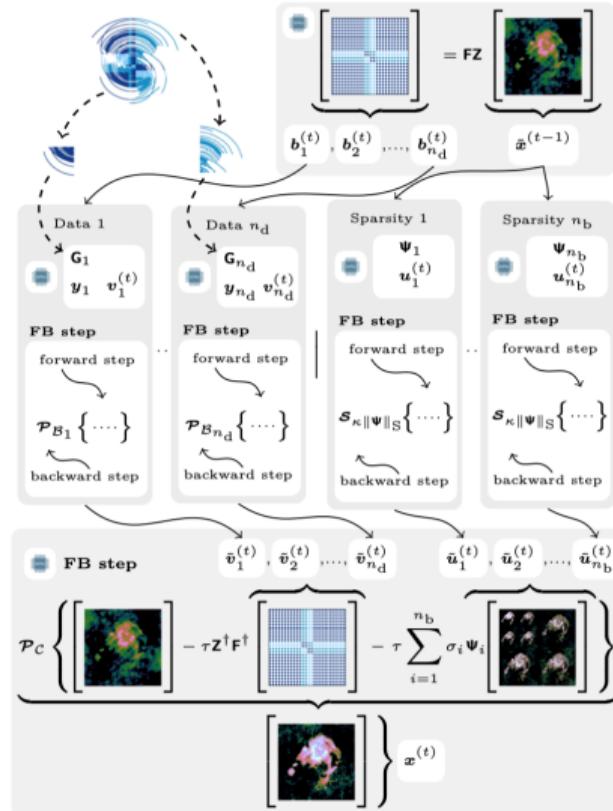
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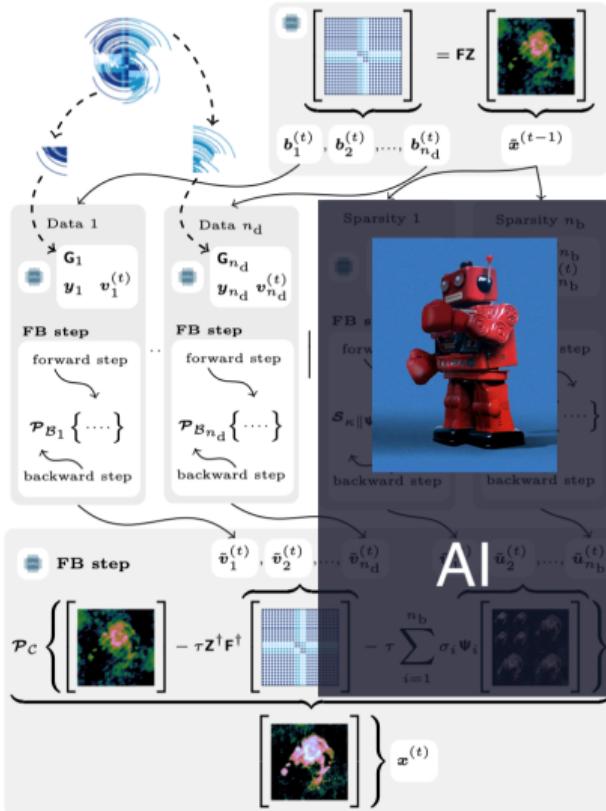
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- ▷ Stochastic updates to support big-data.
- ▷ Two internal distribution strategies:
 1. Distribute image (*i.e.* distribute $\boldsymbol{\Phi}_i$)
 2. Distribute Fourier grid (*i.e.* distribute $\mathbf{G}_i \mathbf{M}_i$)

Block distributed primal dual algorithm



Block distributed primal dual algorithm with AI prior



Exascale Algorithms Uncertainty Quantification

Convex probability concentration for uncertainty quantification

Posterior credible region:

$$p(x \in C_\alpha | y) = \int_{x \in \mathbb{R}^N} p(x|y) \mathbb{1}_{C_\alpha} dx = 1 - \alpha.$$

Consider the highest posterior density (HPD) region

$$C_\alpha^* = \{x : -\log p(x) \leq \gamma_\alpha\}, \quad \text{with } \gamma_\alpha \in \mathbb{R}, \quad \text{and } p(x \in C_\alpha^* | y) = 1 - \alpha \text{ holds.}$$

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Theorem 3.1 (Pereyra 2017)

Suppose the posterior $\log p(x|y) \propto \log \mathcal{L}(x) + \log \pi(x)$ is log-concave on \mathbb{R}^N . Then, for any $\alpha \in (4e^{[-(-N/3)]}, 1)$, the HPD region C_α^* is contained by

$$\hat{C}_\alpha = \left\{ x : \log \mathcal{L}(x) + \log \pi(x) \leq \hat{\gamma}_\alpha = \log \mathcal{L}(\hat{x}_{\text{MAP}}) + \log \pi(\hat{x}_{\text{MAP}}) + \sqrt{N}\tau_\alpha + N \right\},$$

with a positive constant $\tau_\alpha = \sqrt{16 \log(3/\alpha)}$ independent of $p(x|y)$.

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Need only evaluate $\log \mathcal{L} + \log \pi$ for the MAP estimate x_{MAP} !

Local Bayesian credible intervals

Local Bayesian credible intervals for sparse reconstruction

(Cai, Pereyra & McEwen 2018b)

Let Ω define the area (or pixel) over which to compute the credible interval $(\tilde{\xi}_-, \tilde{\xi}_+)$ and ζ be an index vector describing Ω (i.e. $\zeta_i = 1$ if $i \in \Omega$ and 0 otherwise).

Consider the test image with the Ω region replaced by constant value ξ :

$$x' = x^* (\mathcal{I} - \zeta) + \xi \zeta .$$

Given $\tilde{\gamma}_\alpha$ and x^* , compute the credible interval by

$$\tilde{\xi}_- = \min_{\xi} \left\{ \xi \mid \log \mathcal{L}(x') + \log \pi(x') \leq \tilde{\gamma}_\alpha, \forall \xi \in [-\infty, +\infty) \right\},$$

$$\tilde{\xi}_+ = \max_{\xi} \left\{ \xi \mid \log \mathcal{L}(x') + \log \pi(x') \leq \tilde{\gamma}_\alpha, \forall \xi \in [-\infty, +\infty) \right\}.$$

Hypothesis testing

Hypothesis testing of physical structure

(Pereyra 2017; Cai, Pereyra & McEwen 2018a)

1. Remove structure of interest from recovered image x^* .
2. Inpaint background (noise) into region, yielding surrogate image x' .
3. Test whether $x' \in C_\alpha$:
 - ▷ If $x' \notin C_\alpha$ then reject hypothesis that structure is an artefact with confidence $(1 - \alpha)\%$,
i.e. structure most likely physical.
 - ▷ If $x' \in C_\alpha$ uncertainty too high to draw strong conclusions about the physical nature of the structure.

Exascale Algorithms AI Data-Driven Prior

Convex AI prior

Adopt neural-network-based convex regulariser R

(Goujon *et al.* 2022; Liaudat *et al.* McEwen 2024):

$$R(x) = \sum_{n=1}^{N_C} \sum_k \psi_n ((h_n * x)[k]),$$

- ▷ ψ_n are learned convex profile functions with Lipschitz continuous derivative;
- ▷ N_C learned convolutional filters h_n .

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Small-AI but (potentially) Big-Sims.

(Typical PnP learned regularisers also implemented but do not support UQ.)

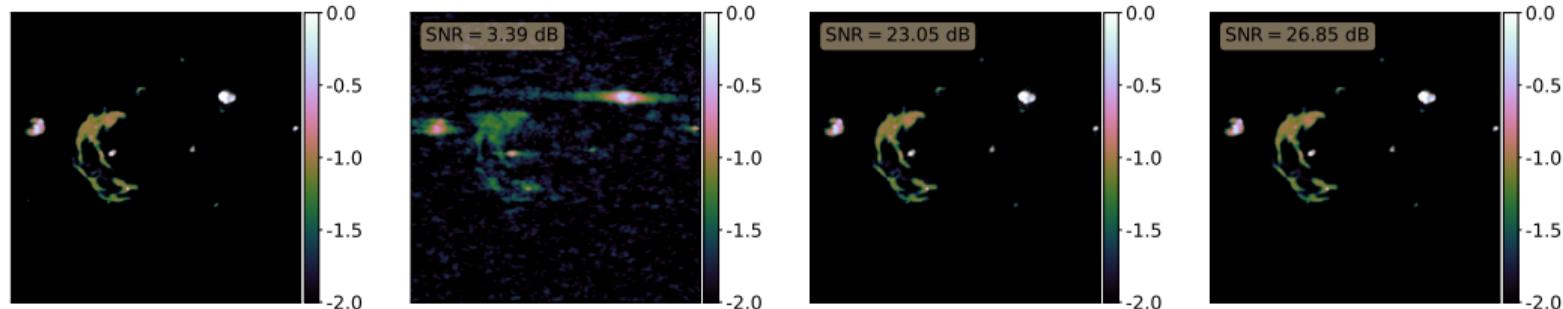
Convex AI prior

Properties:

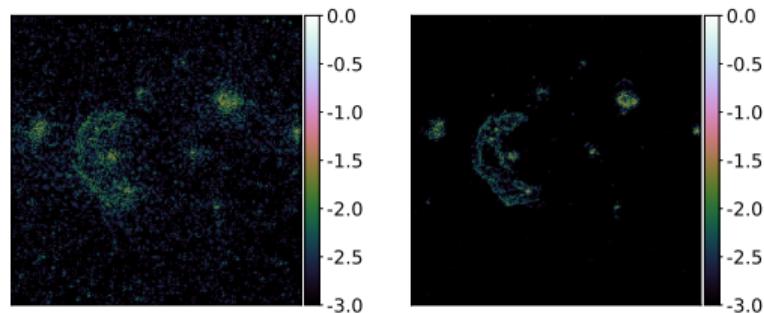
1. Convex + explicit \Rightarrow leverage convex UQ theory.
2. Smooth regulariser with known Lipschitz constant \Rightarrow theoretical convergence guarantees.

Demonstrations

Reconstructed images



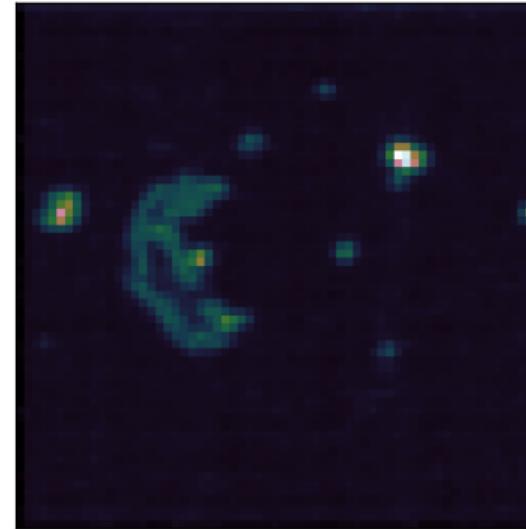
(Liaudat *et al.* McEwen 2024)



Approximate local Bayesian credible intervals



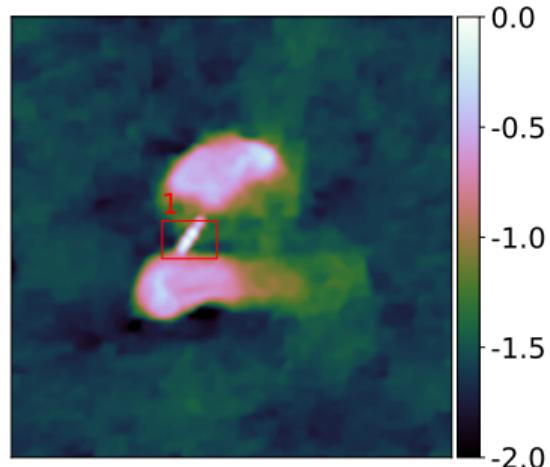
LCI
(super-pixel size 4×4)



MCMC standard deviation
(super-pixel size 4×4)

(Liaudat *et al.* McEwen 2024)

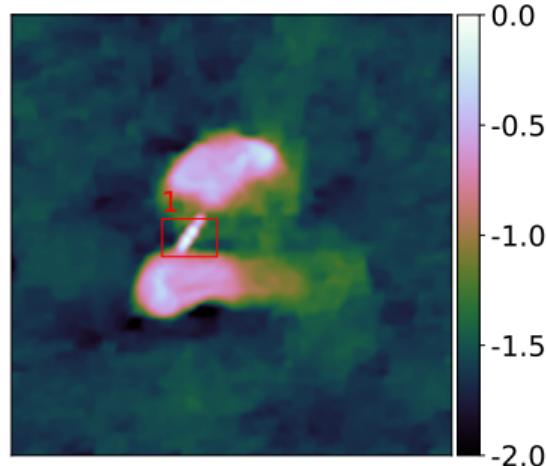
Hypothesis testing of structure



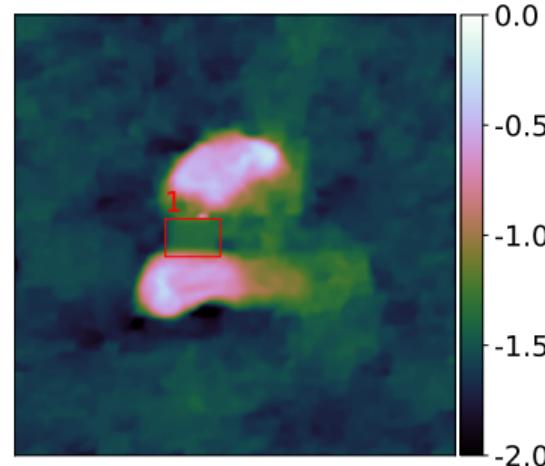
Reconstructed image

(Liaudat *et al.* McEwen 2024)

Hypothesis testing of structure



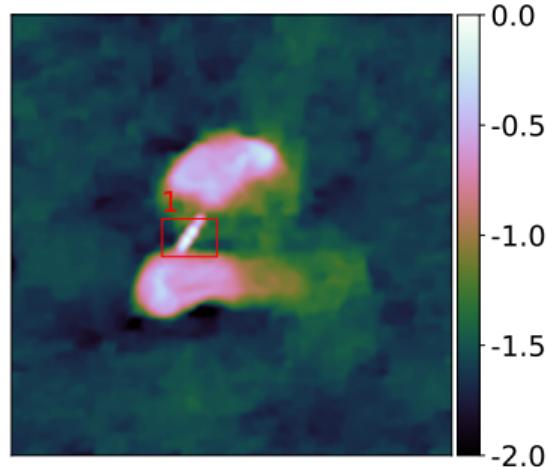
Reconstructed image



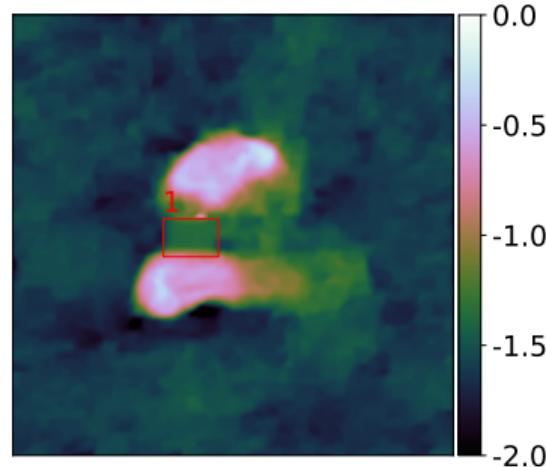
Surrogate test image (region removed)

(Liaudat *et al.* McEwen 2024)

Hypothesis testing of structure



Reconstructed image

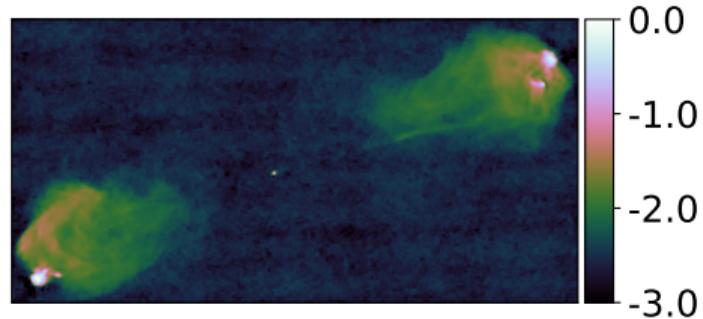


Surrogate test image (region removed)

Reject null hypothesis
⇒ **structure physical**

(Liaudat *et al.* McEwen 2024)

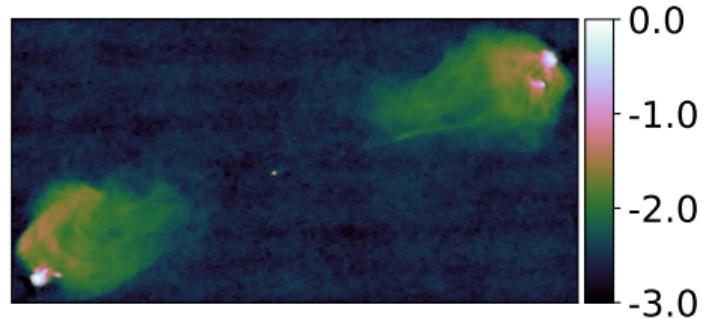
Hypothesis testing of substructure



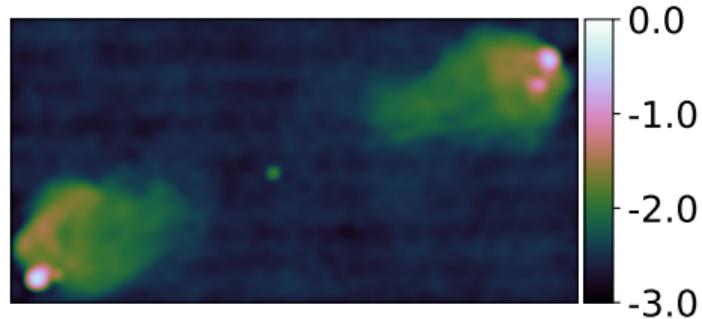
Reconstructed image

(Liaudat *et al.* McEwen 2024)

Hypothesis testing of substructure



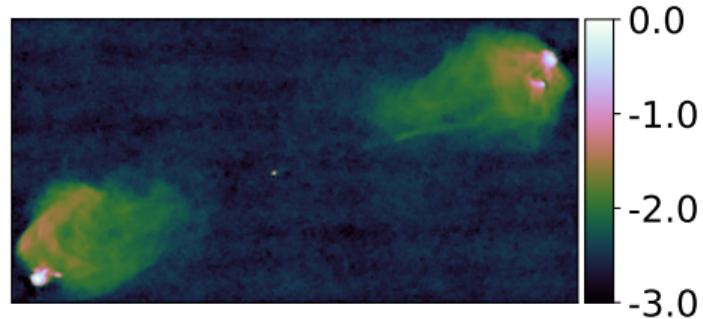
Reconstructed image



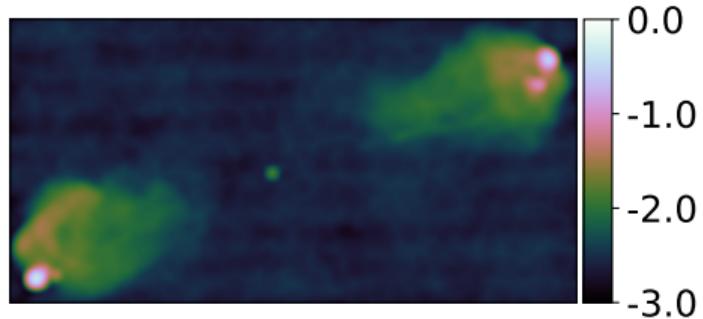
Surrogate test image (blurred)

(Liaudat *et al.* McEwen 2024)

Hypothesis testing of substructure



Reconstructed image

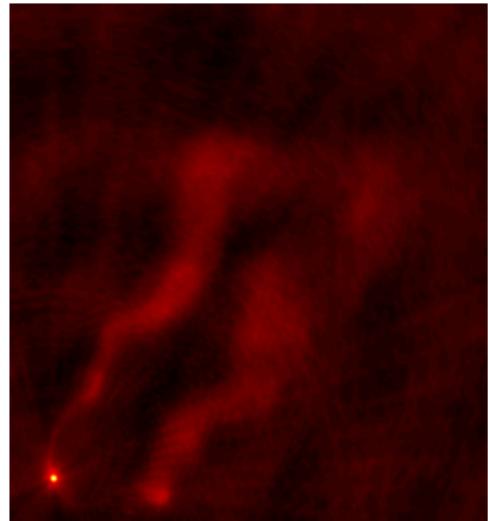


Surrogate test image (blurred)

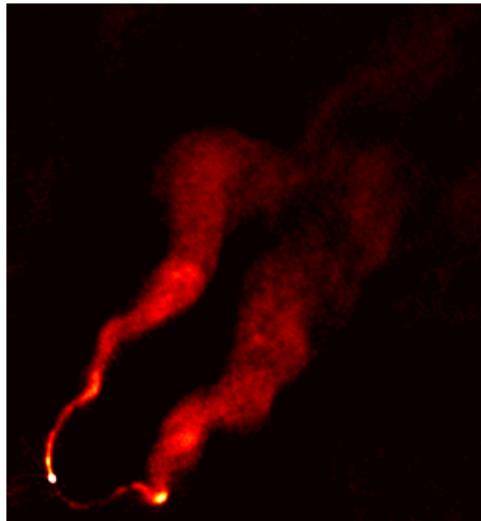
Reject null hypothesis \Rightarrow **substructure physical**

(Liaudat *et al.* McEwen 2024)

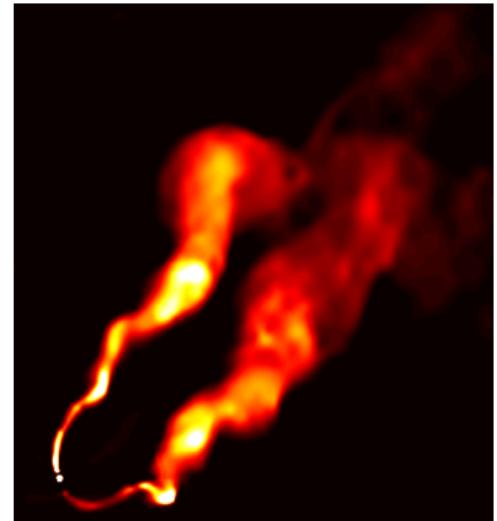
Imaging 3C128 with VLA



Dirty image



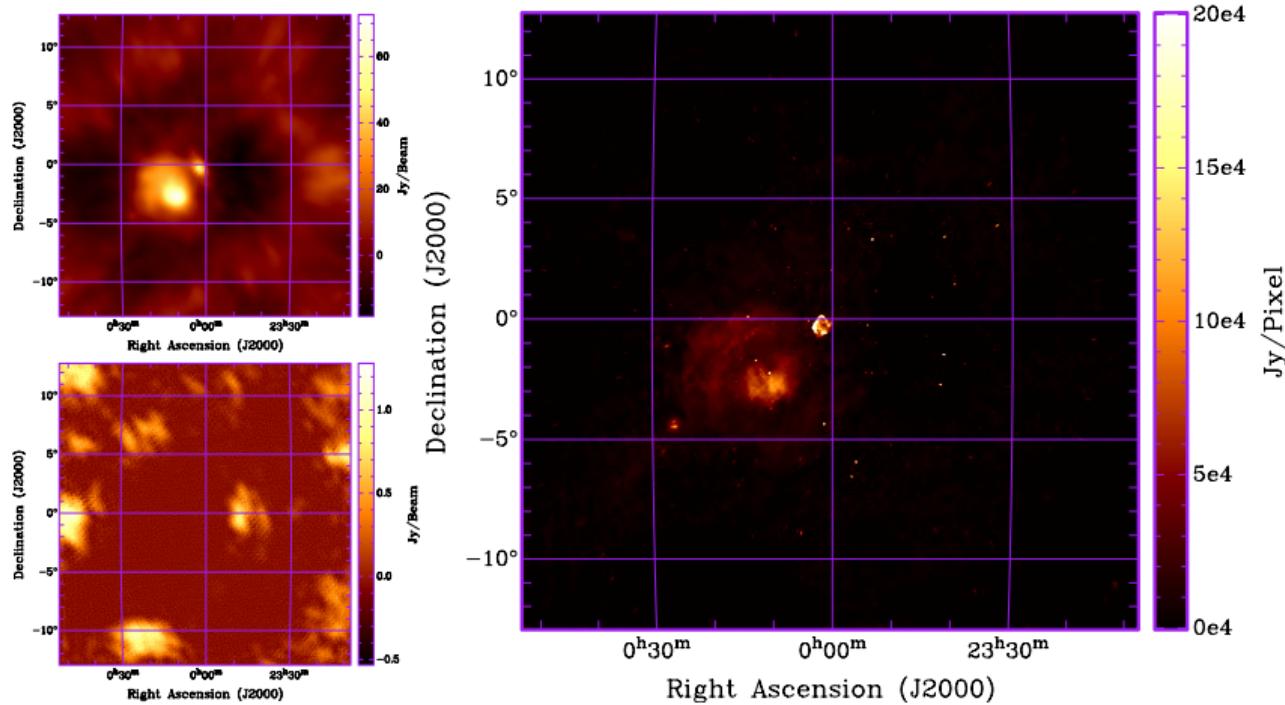
CLEAN



PURIFY (Ours)

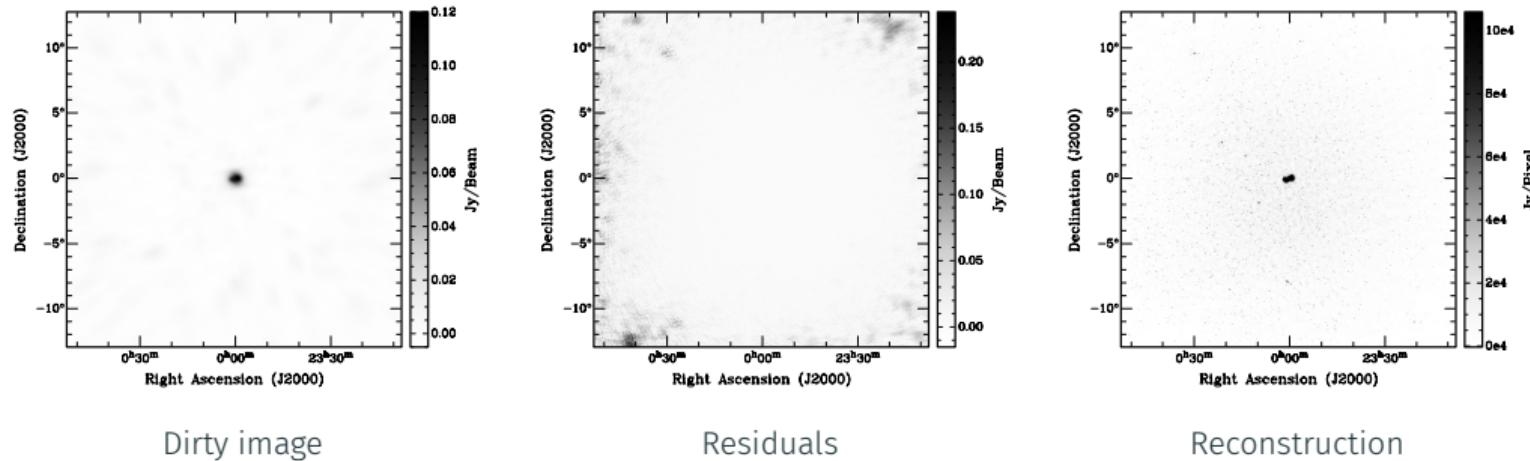
(Pratley, McEwen *et al.* 2018)

Imaging Puppis A with MWA



(Pratley, Johnston-Hollitt & McEwen 2019)

Imaging Fornax A with MWA



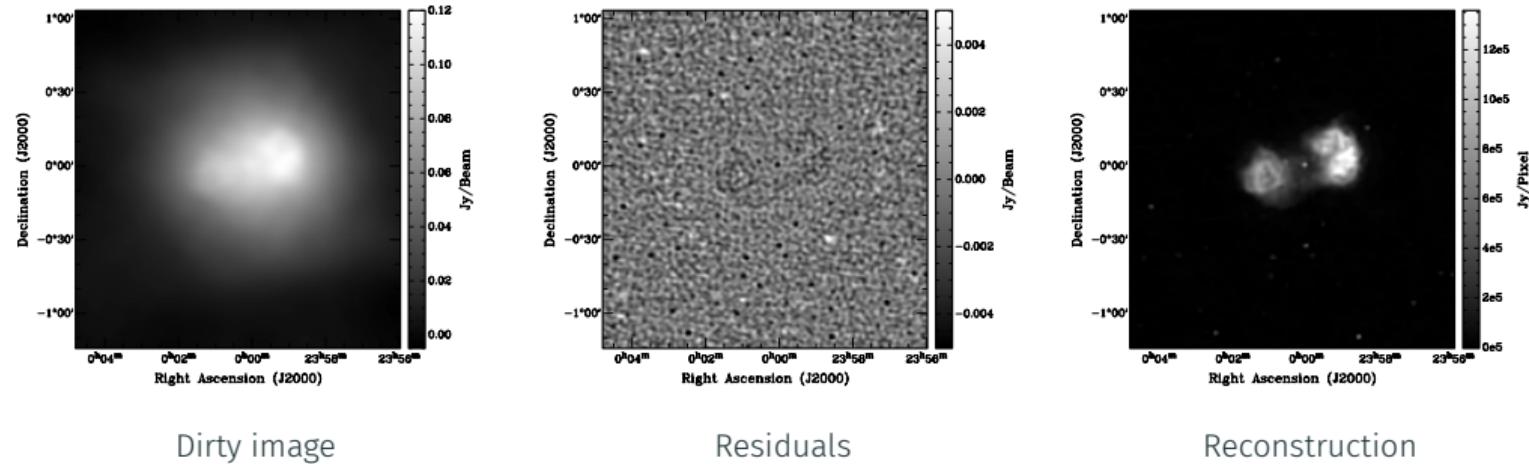
Dirty image

Residuals

Reconstruction

(Pratley, Johnston-Hollitt & McEwen 2020)

Imaging Fornax A with MWA



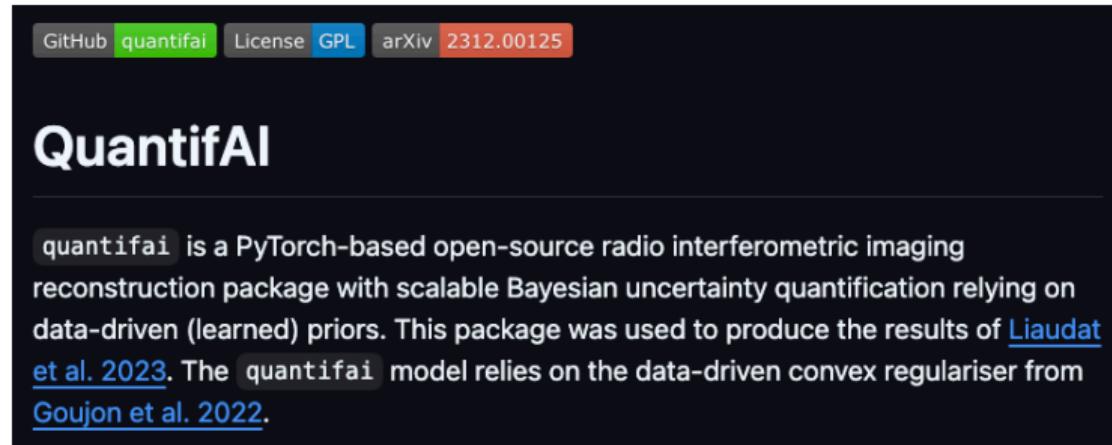
Dirty image

Residuals

Reconstruction

(Pratley, Johnston-Hollitt & McEwen 2020)

QuantifAI code



Github: <https://github.com/astro-informatics/QuantifAI>

PyTorch: Automatic differentiation (including instrument model) + GPU acceleration

Exascale imaging codes

PURIFY

CI passing codecov 86% DOI [10.5281/zenodo.2555252](https://doi.org/10.5281/zenodo.2555252)

Description

PURIFY is an open-source collection of routines written in C++ available under the [license](#) below. It implements different tools and high-level to perform radio interferometric imaging, *i.e.* to recover images from the Fourier measurements taken by radio interferometric telescopes.

GitHub: <https://github.com/astro-informatics/purify>

Sparse OPTimisation Library

CMake passing codecov 96% DOI [10.5281/zenodo.2584256](https://doi.org/10.5281/zenodo.2584256)

Description

SOPT is an open-source C++ package available under the [license](#) below. It performs Sparse OPTimisation using state-of-the-art convex optimisation algorithms. It solves a variety of sparse regularisation problems, including the Sparsity Averaging Reweighted Analysis (SARA) algorithm.

GitHub: <https://github.com/astro-informatics/sopt>

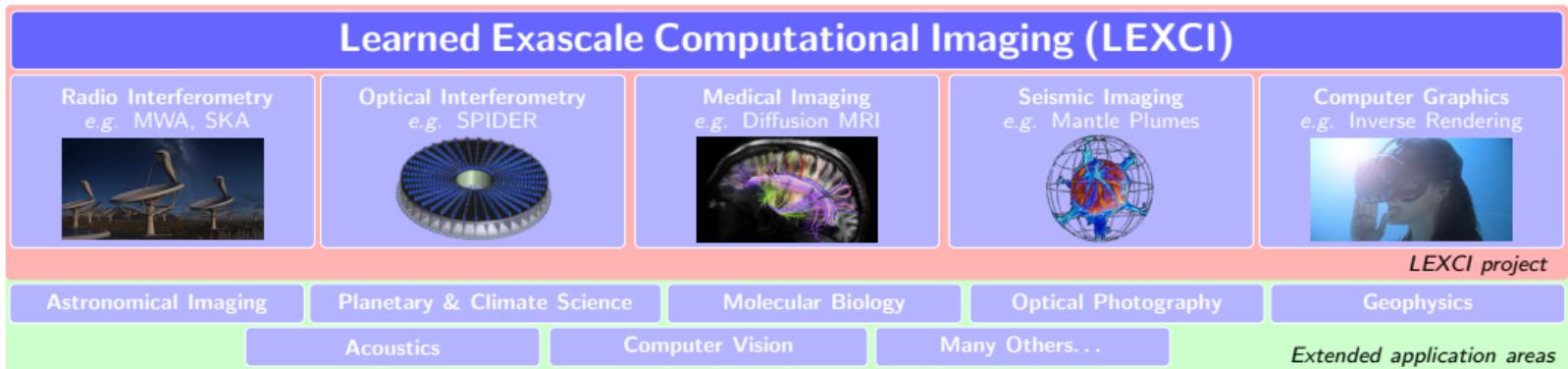


ONNX



Spack

Application domains more broadly



Summary

- ▷ SKA is an exascale radio interferometric imaging experiment
- ▷ Learned exascale computational inverse imaging (LEXCI) framework
 1. Highly distributed and parallelised
 2. Highly realistic telescope modelling (exact wide-field corrections)
 3. Superior reconstruction quality by using learned AI data-driven priors
 4. Uncertainty quantification for exascale imaging with learned priors for the first time.
 5. Validated by MCMC sampling (for low-dimensional setting)
- ▷ Next steps
 1. Benchmark computational performance
 2. Apply full framework to real big-data radio interferometric observations
 3. Other application domains...