Detection of the ISW effect and corresponding dark energy constraints (astro-ph/0602398)

Jason McEwen¹

with P. Vielva^{2,3}, M. P. Hobson¹, E. Martinez-González² and A. N. Lasenby¹

¹Cavendish Laboratory, University of Cambridge 2 Instituto de Física de Cantabria, Universidad de Cantabria ³Laboratoire APC, Collège de France

Rencontres de Moriond :: 23 March 2006

 Ω

Outline

- [Integrated Sachs-Wolfe \(ISW\) effect](#page-2-0)
	- **•** [Physical origin](#page-3-0)
	- [Detecting the effect](#page-7-0)
- 2 [The continuous spherical wavelet transform \(CSWT\)](#page-12-0)
	- [Dilations and mother wavelets on the sphere](#page-13-0)
	- **•** [Transform](#page-17-0)
- 3 [Cross-correlation in wavelet space](#page-21-0)
	- [Wavelet covariance estimator](#page-22-0)
	- [Comparison of wavelets](#page-26-0)
	- 4 [Analysis procedure](#page-30-0)
- **[Results](#page-35-0)**
	- **•** [Detections](#page-36-0)
	- [Dark energy constraints](#page-45-0)

→ 重 ト 4

重き 重 QQ

Outline

- [Integrated Sachs-Wolfe \(ISW\) effect](#page-2-0)
	- **•** [Physical origin](#page-3-0)
	- [Detecting the effect](#page-7-0)
- [The continuous spherical wavelet transform \(CSWT\)](#page-12-0) [Dilations and mother wavelets on the sphere](#page-13-0)
	- [Transform](#page-17-0) \bullet
- 3 [Cross-correlation in wavelet space](#page-21-0)
	- [Wavelet covariance estimator](#page-22-0)
	- [Comparison of wavelets](#page-26-0)
- 4 [Analysis procedure](#page-30-0)
- **[Results](#page-35-0)**
	- **•** [Detections](#page-36-0)
	- [Dark energy constraints](#page-45-0)
- **[Summary](#page-52-0)**

 290

B

医电影 化

G.

- Photons blue (red) shifted when fall into (out of) potential wells
- Evolution of potential during photon propagation \rightarrow net change in photon energy
- Large scale phenomenon (cosmic variance limited \rightarrow require full-sky maps)
- Only present in non-flat universes or flat universes with dark energy

Temperature perturbation

$$
\frac{\delta T}{T} = 2 \int \frac{\dot{\Phi}}{c^2} \frac{d\ell}{c}
$$

where $d\ell$ is the element of proper distance. In Einstein de-Sitter universe (no Λ), $\Phi_k \sim \delta_k/a$ and linear growth law for $\Omega = 1$ is $\delta_k \sim a$. Thus $\dot{\Phi} \neq 0$ only when $Ω$ diverges significantly from unity. イロメ イ伊 メイヨメイヨメー G.

- Photons blue (red) shifted when fall into (out of) potential wells
- Evolution of potential during photon propagation \rightarrow net change in photon energy
- Large scale phenomenon (cosmic variance limited \rightarrow require full-sky maps)
- Only present in non-flat universes or flat universes with dark energy

Temperature perturbation

$$
\frac{\delta T}{T} = 2 \int \frac{\dot{\Phi}}{c^2} \frac{d\ell}{c}
$$

where $d\ell$ is the element of proper distance. In Einstein de-Sitter universe (no Λ), $\Phi_k \sim \delta_k/a$ and linear growth law for $\Omega = 1$ is $\delta_k \sim a$. Thus $\dot{\Phi} \neq 0$ only when $Ω$ diverges significantly from unity. メロトメ 御 トメ 差 トメ 差 トー \Rightarrow

- Photons blue (red) shifted when fall into (out of) potential wells
- Evolution of potential during photon propagation \rightarrow net change in photon energy
- **•** Large scale phenomenon (cosmic variance limited \rightarrow require full-sky maps)
- Only present in non-flat universes or flat universes with dark energy

Temperature perturbation

$$
\frac{\delta T}{T} = 2 \int \frac{\dot{\Phi}}{c^2} \frac{d\ell}{c}
$$

where $d\ell$ is the element of proper distance. In Einstein de-Sitter universe (no Λ), $\Phi_k \sim \delta_k/a$ and linear growth law for $\Omega = 1$ is $\delta_k \sim a$. Thus $\dot{\Phi} \neq 0$ only when $Ω$ diverges significantly from unity. イロト イ押 トイヨ トイヨ トー \Rightarrow

- Photons blue (red) shifted when fall into (out of) potential wells
- Evolution of potential during photon propagation \rightarrow net change in photon energy
- **•** Large scale phenomenon (cosmic variance limited \rightarrow require full-sky maps)
- Only present in non-flat universes or flat universes with dark energy

Temperature perturbation

$$
\frac{\delta T}{T}=2\int\frac{\dot{\Phi}}{c^2}\frac{\text{d}\ell}{c}
$$

where $d\ell$ is the element of proper distance. In Einstein de-Sitter universe (no Λ), $\Phi_k \sim \delta_k/a$ and linear growth law for $\Omega = 1$ is $\delta_k \sim a$. Thus $\dot{\Phi} \neq 0$ only when Ω diverges significantly from unity. イロメ イ伊 メイヨメイヨメー \Rightarrow

• Cannot directly separate the ISW signal from CMB anisotropies

- Detected by cross-correlating CMB anisotropies with tracers of large scale structure (Crittenden & Turok 1996)
- Detections used to place constraints on dark energy
- **•** Previous works
	- Real space angular correlation function (e.g. Boughn & Crittenden 2002)
	- Harmonic space cross-angular power spectrum (e.g. Afshordi et al. 2004)
	- Azimuthally symmetric wavelet covariance (Vielva et al. 2006)
- We extend spherical wavelet approach to directional wavelets (no reason to expect azimuthally symmetric structures)

K ロ ト K 何 ト K ヨ ト K ヨ ト

- Cannot directly separate the ISW signal from CMB anisotropies
- Detected by cross-correlating CMB anisotropies with tracers of large scale structure (Crittenden & Turok 1996)
- Detections used to place constraints on dark energy
- **•** Previous works
	- Real space angular correlation function (e.g. Boughn & Crittenden 2002)
	- Harmonic space cross-angular power spectrum (e.g. Afshordi et al. 2004)
	- Azimuthally symmetric wavelet covariance (Vielva et al. 2006)
- We extend spherical wavelet approach to directional wavelets (no reason to expect azimuthally symmetric structures)

イロメ イ伊 メイヨメイヨメー

- Cannot directly separate the ISW signal from CMB anisotropies
- Detected by cross-correlating CMB anisotropies with tracers of large scale structure (Crittenden & Turok 1996)
- Detections used to place constraints on dark energy
- **•** Previous works
	- Real space angular correlation function (e.g. Boughn & Crittenden 2002)
	- Harmonic space cross-angular power spectrum (e.g. Afshordi et al. 2004)
	- Azimuthally symmetric wavelet covariance (Vielva et al. 2006)
- We extend spherical wavelet approach to directional wavelets (no reason to expect azimuthally symmetric structures)

イロメ イ伊 メイヨメイヨメー

- Cannot directly separate the ISW signal from CMB anisotropies
- Detected by cross-correlating CMB anisotropies with tracers of large scale structure (Crittenden & Turok 1996)
- Detections used to place constraints on dark energy
- **•** Previous works
	- Real space angular correlation function (e.g. Boughn & Crittenden 2002)
	- Harmonic space cross-angular power spectrum (e.g. Afshordi et al. 2004)
	- Azimuthally symmetric wavelet covariance (Vielva et al. 2006)
- We extend spherical wavelet approach to directional wavelets (no reason to expect azimuthally symmetric structures)

イロト イ団ト イヨト イヨト

重

- Cannot directly separate the ISW signal from CMB anisotropies
- Detected by cross-correlating CMB anisotropies with tracers of large scale structure (Crittenden & Turok 1996)
- Detections used to place constraints on dark energy
- **•** Previous works
	- Real space angular correlation function (e.g. Boughn & Crittenden 2002)
	- Harmonic space cross-angular power spectrum (e.g. Afshordi et al. 2004)
	- Azimuthally symmetric wavelet covariance (Vielva et al. 2006)
- We extend spherical wavelet approach to directional wavelets (no reason to expect azimuthally symmetric structures)

イロト イ団ト イヨト イヨト

重

伊 ▶ イヨ ▶ イヨ ▶

重

 $2Q$

Outline

- [Integrated Sachs-Wolfe \(ISW\) effect](#page-2-0)
	- [Physical origin](#page-3-0) \bullet
	- [Detecting the effect](#page-7-0) \bullet
- 2 [The continuous spherical wavelet transform \(CSWT\)](#page-12-0) • [Dilations and mother wavelets on the sphere](#page-13-0) **•** [Transform](#page-17-0)
	- 3 [Cross-correlation in wavelet space](#page-21-0)
		- [Wavelet covariance estimator](#page-22-0)
		- [Comparison of wavelets](#page-26-0)
- 4 [Analysis procedure](#page-30-0)
- **[Results](#page-35-0)**
	- **•** [Detections](#page-36-0)
	- [Dark energy constraints](#page-45-0)
- **[Summary](#page-52-0)**

K 何 ▶ K ヨ ▶ K ヨ ▶ ..

净

 $2Q$

Spherical wavelet transform Anisotropic dilation on the sphere

- Spherical wavelet transform (Antoine and Vandergheynst 1998; Wiaux et al. 2005)
- Stereographic projection Π
- Anisotropic dilation on the sphere

 $D(a, b) = \Pi^{-1} d(a, b) \Pi$

$$
[\mathcal{D}(a,b)s](\omega)=[\lambda(a,b,\theta,\phi)]^{1/2} s(\omega_{1/a,1/b})
$$

where

$$
\omega_{a,b} = (\theta_{a,b}, \phi_{a,b}),
$$

\n
$$
\tan(\theta_{a,b}/2) = \tan(\theta/2)\sqrt{a^2 \cos^2 \phi + b^2 \sin^2 \phi}
$$

\n
$$
\tan(\phi_{a,b}) = \frac{b}{a} \tan(\phi)
$$

Spherical wavelet transform Anisotropic dilation on the sphere

- Spherical wavelet transform (Antoine and Vandergheynst 1998; Wiaux et al. 2005)
- Stereographic projection Π
- Anisotropic dilation on the sphere $D(a, b) = \Pi^{-1} d(a, b) \Pi$

$$
[\mathcal{D}(a,b)s](\omega)=[\lambda(a,b,\theta,\phi)]^{1/2} s(\omega_{1/a,1/b})
$$

where

$$
\omega_{a,b} = (\theta_{a,b}, \phi_{a,b}),
$$

\n
$$
\tan(\theta_{a,b}/2) = \tan(\theta/2)\sqrt{a^2 \cos^2 \phi + b^2 \sin^2 \phi}
$$

\n
$$
\tan(\phi_{a,b}) = \frac{b}{a} \tan(\phi)
$$

 $\langle \oplus \rangle$ > $\langle \oplus \rangle$ > $\langle \oplus \rangle$

 290

重

Spherical wavelet transform Anisotropic dilation on the sphere

- Spherical wavelet transform (Antoine and Vandergheynst 1998; Wiaux et al. 2005)
- Stereographic projection Π
- Anisotropic dilation on the sphere

 $\mathcal{D}(a,b)=\Pi^{-1}d(a,b)\Pi$

$$
[\mathcal{D}(a,b)s](\omega)=[\lambda(a,b,\theta,\phi)]^{1/2}\,\mathbf{s}(\omega_{1/a,1/b})
$$

where

$$
\omega_{a,b} = (\theta_{a,b}, \phi_{a,b}),
$$

\n
$$
\tan(\theta_{a,b}/2) = \tan(\theta/2)\sqrt{a^2 \cos^2 \phi + b^2 \sin^2 \phi}
$$

\n
$$
\tan(\phi_{a,b}) = \frac{b}{a} \tan(\phi)
$$

←何 → → ヨ →

重

 QQ

イロト イ団ト イヨト イヨト

(B) 2990

Spherical wavelet transform Mother wavelets on the sphere

• Stereographic projection of admissible Euclidean mother wavelets

$$
\psi(\omega)=[\Pi^{-1}\psi_{\mathbb{R}^2}](\omega)
$$

Figure: Spherical wavelets at scale $a = b = 0.2$.

イロト イ団ト イヨト イヨト

重

 QQ

Spherical wavelet transform

• Motion on the sphere (\equiv rotation)

$$
[R(\rho)s](\omega) = s(\rho^{-1}\omega), \ \rho \in \mathrm{SO}(3)
$$

• Multi-resolution basis on the sphere

 $\{\psi_{a,b,\rho} \equiv R(\rho)\mathcal{D}(a,b)\psi; \ \rho \in SO(3); \ a,b \in \mathbb{R}^+_*\}$

• Spherical wavelet transform

$$
W_{\psi}(a,b,\rho) \equiv \int_{S^2} d\Omega(\omega) \, \psi_{a,b,\rho}^*(\omega) \, s(\omega)
$$

メ都 メメミメメ ミメー

净

 QQ

4 0 8

Spherical wavelet transform

• Motion on the sphere (\equiv rotation)

$$
[R(\rho)s](\omega) = s(\rho^{-1}\omega), \ \rho \in \mathrm{SO}(3)
$$

• Multi-resolution basis on the sphere

$$
\{\psi_{a,b,\rho}\equiv R(\rho)\mathcal{D}(a,b)\psi;\ \rho\in\mathrm{SO}(3);\ a,b\in\mathbb{R}^+_*\}
$$

• Spherical wavelet transform

$$
W_{\psi}(a,b,\rho) \equiv \int_{S^2} d\Omega(\omega) \, \psi^*_{a,b,\rho}(\omega) \, s(\omega)
$$

K 何 ▶ K ヨ ▶ K ヨ ▶ ...

净

 QQ

Spherical wavelet transform

• Motion on the sphere (\equiv rotation)

$$
[R(\rho) s](\omega) = s(\rho^{-1}\omega), \ \rho \in \mathrm{SO}(3)
$$

• Multi-resolution basis on the sphere

$$
\{\psi_{a,b,\rho}\equiv R(\rho)\mathcal{D}(a,b)\psi;\ \rho\in\mathrm{SO}(3);\ a,b\in\mathbb{R}^+_*\}
$$

• Spherical wavelet transform

$$
\mathsf{W}_{\psi}(a,b,\rho)\equiv\int_{S^2}\,\mathrm{d}\Omega(\omega)\,\psi^*_{a,b,\rho}(\omega)\,\mathsf{s}(\omega)
$$

K 何 ト K ヨ ト K ヨ ト

净

 QQ

Spherical wavelet transform

• Motion on the sphere (\equiv rotation)

$$
[R(\rho)s](\omega) = s(\rho^{-1}\omega), \ \rho \in \mathrm{SO}(3)
$$

• Multi-resolution basis on the sphere

$$
\{\psi_{a,b,\rho}\equiv R(\rho)\mathcal{D}(a,b)\psi;\ \rho\in\mathrm{SO}(3);\ a,b\in\mathbb{R}^+_*\}
$$

• Spherical wavelet transform

$$
W_{\psi}(a,b,\rho)\equiv\int_{S^2}\,\mathrm{d}\Omega(\omega)\,\psi^*_{a,b,\rho}(\omega)\,s(\omega)
$$

医电子 化重子

A P

G.

 $2Q$

Outline

- [Integrated Sachs-Wolfe \(ISW\) effect](#page-2-0)
	- **[Physical origin](#page-3-0)**
	- [Detecting the effect](#page-7-0) \bullet
- [The continuous spherical wavelet transform \(CSWT\)](#page-12-0) [Dilations and mother wavelets on the sphere](#page-13-0)
	- [Transform](#page-17-0) \bullet
- 3 [Cross-correlation in wavelet space](#page-21-0)
	- [Wavelet covariance estimator](#page-22-0)
	- [Comparison of wavelets](#page-26-0)
	- 4 [Analysis procedure](#page-30-0)
- **[Results](#page-35-0)**
	- **•** [Detections](#page-36-0)
	- [Dark energy constraints](#page-45-0)
- **[Summary](#page-52-0)**

画

 $2Q$

K 何 ▶ K ヨ ▶ K ヨ ▶ ...

Wavelet covariance estimator

- Suitability of wavelets for detecting cross-correlations
- Wavelet covariance

$$
\hat{X}_{\psi}^{\text{NT}}(a,b,\gamma)=\frac{1}{N_{\alpha\beta}}\sum_{\alpha,\beta}\nu_{\alpha\beta}W_{\psi}^{\text{N}}(a,b,\alpha,\beta,\gamma)W_{\psi}^{\text{T}}(a,b,\alpha,\beta,\gamma)
$$

• Average over orientations

$$
\hat{X}^{\mathrm{NT}}_{\psi}(a,b)=\frac{1}{N_{\gamma}}\sum_{\gamma}\ \hat{X}^{\mathrm{NT}}_{\psi}(a,b,\gamma)
$$

$$
X^{\mathrm{NT}}_\psi(a,b,\gamma) = \sum_{\ell=0}^\infty \, {p_\ell}^2 \, {b^{\mathrm{N}}_\ell} \, {b^{\mathrm{T}}_\ell} \, {C^{\mathrm{NT}}_\ell} \sum_{m=-\ell}^\ell \big| (\psi_{a,b})_{\ell m} \big|^2
$$

K 何 ト K ヨ ト K ヨ ト

净

 $2Q$

Wavelet covariance estimator

- Suitability of wavelets for detecting cross-correlations
- Wavelet covariance

$$
\hat{X}_{\psi}^{\rm NT}(a,b,\gamma)=\frac{1}{N_{\alpha\beta}}\sum_{\alpha,\beta}\nu_{\alpha\beta}W_{\psi}^{\rm N}(a,b,\alpha,\beta,\gamma)W_{\psi}^{\rm T}(a,b,\alpha,\beta,\gamma)
$$

• Average over orientations

$$
\hat{X}^{\mathrm{NT}}_{\psi}(a,b)=\frac{1}{N_{\gamma}}\sum_{\gamma}\,\hat{X}^{\mathrm{NT}}_{\psi}(a,b,\gamma)
$$

$$
X^{\mathrm{NT}}_\psi(a,b,\gamma) = \sum_{\ell=0}^\infty \, p_\ell{}^2 \, b_\ell^\mathrm{N} \, b_\ell^\mathrm{T} \, C_\ell^\mathrm{NT} \sum_{m=-\ell}^\ell \big| (\psi_{a,b})_{\ell m} \big|^2
$$

K 何 ▶ K ヨ ▶ K ヨ ▶ ...

净

 QQ

Wavelet covariance estimator

- Suitability of wavelets for detecting cross-correlations
- Wavelet covariance

$$
\hat{X}_{\psi}^{\rm NT}(a,b,\gamma)=\frac{1}{N_{\alpha\beta}}\sum_{\alpha,\beta}\nu_{\alpha\beta}W_{\psi}^{\rm N}(a,b,\alpha,\beta,\gamma)W_{\psi}^{\rm T}(a,b,\alpha,\beta,\gamma)
$$

• Average over orientations

$$
\hat{X}_{\psi}^{\rm NT}(a,b)=\frac{1}{N_{\gamma}}\sum_{\gamma}\ \hat{X}_{\psi}^{\rm NT}(a,b,\gamma)
$$

$$
X^{\mathrm{NT}}_\psi(a,b,\gamma) = \sum_{\ell=0}^\infty \, {p_\ell}^2 \, {b^{\mathrm{N}}_\ell} \, {b^{\mathrm{T}}_\ell} \, {C^{\mathrm{NT}}_\ell} \sum_{m=-\ell}^\ell \big| (\psi_{a,b})_{\ell m} \big|^2
$$

伊 ▶ イヨ ▶ イヨ ▶

净

 QQ

Wavelet covariance estimator

- Suitability of wavelets for detecting cross-correlations
- Wavelet covariance

$$
\hat{X}_{\psi}^{\rm NT}(a,b,\gamma)=\frac{1}{N_{\alpha\beta}}\sum_{\alpha,\beta}\nu_{\alpha\beta}W_{\psi}^{\rm N}(a,b,\alpha,\beta,\gamma)W_{\psi}^{\rm T}(a,b,\alpha,\beta,\gamma)
$$

• Average over orientations

$$
\hat{X}_{\psi}^{\rm NT}(a,b)=\frac{1}{N_{\gamma}}\sum_{\gamma}\ \hat{X}_{\psi}^{\rm NT}(a,b,\gamma)
$$

$$
X^{\mathrm{NT}}_\psi(a,b,\gamma) = \sum_{\ell=0}^\infty \, \rho_\ell{}^2 \, b_\ell^\mathrm{N} \, b_\ell^\mathrm{T} \, C^{\mathrm{NT}}_\ell \, \sum_{m=-\ell}^\ell \big| (\psi_{a,b})_{\ell m} \big|^2
$$

Comparison of wavelets

• Compare predicted signal-to-noise ratio

$$
\mathrm{SNR}_{\psi}(a,b) = \frac{\left<\hat{X}_{\psi}^{\mathrm{NT}}(a,b)\right>}{\Delta \hat{X}_{\psi}^{\mathrm{NT}}(a,b)}
$$

where

$$
\left[\Delta\hat{X}_{\psi}^{\mathrm{NT}}(a,b)\right]^2=\sum_{\ell=0}^{\infty}\frac{1}{2\ell+1}\,\rho_{\ell}^{4}\,(b_{\ell}^{\mathrm{N}})^2\,(b_{\ell}^{\mathrm{T}})^2\,\left[\sum_{m=-\ell}^{\ell}\left|(\psi_{a,b})_{\ell m}\right|^2\right]^2\left[(C_{\ell}^{\mathrm{NT}})^2+C_{\ell}^{\mathrm{TT}}C_{\ell}^{\mathrm{NN}}\right]
$$

- Similar technique used to compare real, harmonic and wavelet space techniques for detection of cross-correlations
	- \rightarrow wavelets optimal on certain scales (Vielva et al. 2006)

メラト メミト メミト

重

 QQ

Comparison of wavelets

• Compare predicted signal-to-noise ratio

$$
\mathrm{SNR}_{\psi}(a,b) = \frac{\left<\hat{X}_{\psi}^{\mathrm{NT}}(a,b)\right>}{\Delta \hat{X}_{\psi}^{\mathrm{NT}}(a,b)}
$$

where

$$
\left[\Delta \hat{X}_{\psi}^{\text{NT}}(a,b)\right]^2 = \sum_{\ell=0}^{\infty} \frac{1}{2\ell+1} \; \rho_{\ell}^{\;4} \left(b_{\ell}^{\text{N}}\right)^2 \left(b_{\ell}^{\text{T}}\right)^2 \; \left[\sum_{m=-\ell}^{\ell} \left|(\psi_{a,b})_{\ell m}\right|^2\right]^2 \left[(C_{\ell}^{\text{NT}})^2 + C_{\ell}^{\text{TT}} C_{\ell}^{\text{NN}}\right]
$$

Similar technique used to compare real, harmonic and wavelet space techniques for detection of cross-correlations

 \rightarrow wavelets optimal on certain scales (Vielva et al. 2006)

K 何 ▶ K ヨ ▶ K ヨ ▶ ...

净

 QQ

← 中 →

4 0 8

→ 重 ★

G.

重き

 \sim

 2990

Comparison of wavelets SNR plots

Figure: Expected SNR of the wavelet covariance estimator of CMB and radio source maps

• Don't consider SMW further (actually considered; as expected not effective)

画

B \mathbf{p}

× → 重 ⊁ 2990

Comparison of wavelets SNR plots

Figure: Expected SNR of the wavelet covariance estimator of CMB and radio source maps

• Don't consider SMW further (actually considered; as expected not effective)

Outline

- [Integrated Sachs-Wolfe \(ISW\) effect](#page-2-0)
	- **[Physical origin](#page-3-0)**
	- [Detecting the effect](#page-7-0) \bullet
- [The continuous spherical wavelet transform \(CSWT\)](#page-12-0)
	- [Dilations and mother wavelets on the sphere](#page-13-0) \bullet
	- **•** [Transform](#page-17-0)
- 3 [Cross-correlation in wavelet space](#page-21-0)
	- [Wavelet covariance estimator](#page-22-0)
	- [Comparison of wavelets](#page-26-0)

4 [Analysis procedure](#page-30-0)

- **[Results](#page-35-0)**
	- **•** [Detections](#page-36-0)
	- [Dark energy constraints](#page-45-0)
- **[Summary](#page-52-0)**

B

- 4 周 8 34

G.

4 0 8

 $\langle \oplus \rangle$ > $\langle \oplus \rangle$ > $\langle \oplus \rangle$

 2990

重

- Analysis (scales; masks)
- **•** Simulations
- Constraints on dark energy parameters

WMAP1 NVSS

4 0 8

4 個 ▶ 4 ヨ ▶ 4

G.

重き

- Analysis (scales; masks)
- **•** Simulations
- Constraints on dark energy parameters

WMAP1 NVSS

4 0 8

 \sqrt{m} > \sqrt{m} > \sqrt{m}

B

重

- Analysis (scales; masks)
- **•** Simulations
- Constraints on dark energy parameters

- Analysis (scales; masks)
- **•** Simulations
- **Constraints on dark energy parameters**

4 0 8

K 何 ▶ ス ヨ ▶

 2990

重

э

医电子 化重子

A P

G.

 $2Q$

Outline

- [Integrated Sachs-Wolfe \(ISW\) effect](#page-2-0)
	- **[Physical origin](#page-3-0)**
	- [Detecting the effect](#page-7-0) \bullet
- [The continuous spherical wavelet transform \(CSWT\)](#page-12-0)
	- [Dilations and mother wavelets on the sphere](#page-13-0) \bullet
	- [Transform](#page-17-0) \bullet
- 3 [Cross-correlation in wavelet space](#page-21-0)
	- [Wavelet covariance estimator](#page-22-0)
	- [Comparison of wavelets](#page-26-0)
	- 4 [Analysis procedure](#page-30-0)
- **[Results](#page-35-0)**
	- **•** [Detections](#page-36-0)
	- [Dark energy constraints](#page-45-0)

[Summary](#page-52-0)

Scales and detections

o Scales

• Wavelet covariance plots

Jason McEwen [Detection of the ISW effect](#page-0-0)

4日下

唐

メ御 ドメ 君 ドメ 君 ドー

Scales and detections

o Scales

• Wavelet covariance plots

4日)

同 × \langle 唐

ほんする

Significance of detections

• Most significant detections

- Wavelet covariance statistics appear Gaussian
	- \rightarrow N_{σ} direct indication of significance of detections
- **symmetric SMHW: 3.6** σ **; elliptical SMHW: 3.9** σ **; SBW: 3.9** σ

• N_{σ} plots (2 and 3 σ contours)

 $\langle \oplus \rangle$ > $\langle \oplus \rangle$ > $\langle \oplus \rangle$

重

 QQ

Significance of detections

- Most significant detections
	- Wavelet covariance statistics appear Gaussian
		- \rightarrow N_{σ} direct indication of significance of detections
	- **symmetric SMHW: 3.6** σ **; elliptical SMHW: 3.9** σ **: SBW: 3.9** σ

• N_{σ} plots (2 and 3 σ contours)

 $\langle \oplus \rangle$ > $\langle \oplus \rangle$ > $\langle \oplus \rangle$

 QQ

遥

Significance of detections

- Most significant detections
	- Wavelet covariance statistics appear Gaussian
		- \rightarrow N_{σ} direct indication of significance of detections
	- **symmetric SMHW: 3.6** σ **; elliptical SMHW: 3.9** σ **; SBW: 3.9** σ
- N_{σ} plots (2 and 3 σ contours)

Systematics and foregrounds

- Systematics: individual WMAP receiver maps
	- \rightarrow systematics not likely source of detection
- Foregrounds: foreground dominated difference maps \rightarrow foregrounds not likely source of detection

Localised regions **Detection**

- Wavelets inherently provide spatial localisation (in addition to scale localisation)
- Threshold wavelet coefficient product maps to localise most likely sources

イロト イ押 トイヨ トイヨト

重

Localised regions **Detection**

- Wavelets inherently provide spatial localisation (in addition to scale localisation)
- Threshold wavelet coefficient product maps to localise most likely sources

G.

伊 ▶ ィミ ▶ :

Localised regions **Removal**

• Remove localised regions \rightarrow ISW detection remains (Agrees with findings of Boughn and Crittenden 2004)

• Examined localised regions in closer detail

 290

 \sim

Dark energy constraints

• Compute theoretical wavelet covariance for range of models (w, Ω_Λ)

(assume concordance model for other parameters; bias $b = 1.6$)

• Compare theoretical predictions with observations

 $\chi^2(w, \Omega_\Lambda) = \Delta^\mathrm{T} C^{-1} \Delta$

where

$$
\Delta = [\hat{X}^{\mathrm{NT}}_{\psi}(a,b,\gamma)-X^{\mathrm{NT}}_{\psi}(a,b,\gamma|w,\Omega_{\Lambda})]
$$

• Compute likelihood

 $\mathcal{L}(w,\Omega_{\Lambda})\propto \mathsf{exp}[-\chi^2(w,\Omega_{\Lambda})/2]$

◆ロ→ ◆伊→ ◆ミ→ →ミ→ → ミ

Dark energy constraints

• Compute theoretical wavelet covariance for range of models (w, Ω_Λ)

(assume concordance model for other parameters; bias $b = 1.6$)

• Compare theoretical predictions with observations

$$
\chi^2(w,\Omega_\Lambda)=\Delta^T\textbf{C}^{-1}\Delta
$$

where

$$
\Delta = [\hat{X}^{\mathrm{NT}}_{\psi}(a,b,\gamma) - X^{\mathrm{NT}}_{\psi}(a,b,\gamma | \textit{\textbf{w}}, \Omega_{\Lambda})]
$$

• Compute likelihood

 $\mathcal{L}(w,\Omega_{\Lambda})\propto \mathsf{exp}[-\chi^2(w,\Omega_{\Lambda})/2]$

イロト イ伊 トイヨ トイヨ トーヨー

Dark energy constraints

• Compute theoretical wavelet covariance for range of models (w, Ω_Λ)

(assume concordance model for other parameters; bias $b = 1.6$)

• Compare theoretical predictions with observations

$$
\chi^2(w,\Omega_\Lambda)=\Delta^{\rm T} C^{-1}\Delta
$$

where

$$
\Delta = [\hat{X}^{\mathrm{NT}}_{\psi}(a,b,\gamma) - X^{\mathrm{NT}}_{\psi}(a,b,\gamma | \textit{\textbf{w}}, \Omega_{\Lambda})]
$$

• Compute likelihood

$$
\mathcal{L}(w,\Omega_\Lambda) \propto \text{exp}[-\chi^2(w,\Omega_\Lambda)/2]
$$

K 何 ▶ K ヨ ▶ K ヨ ▶ ...

净

 QQ

Dark energy constraints Likelihood surfaces

Parameter estimates from mean of marginalised distributions

- $Ω_\Lambda = 0.63_{-0.17}^{+0.18}; w = -0.77_{-0.36}^{+0.35}$ using SMHW
- $Ω_\Lambda = 0.52^{+0.20}_{-0.20}; w = -0.73^{+0.42}_{-0.46}$ using SBW

K ロ ▶ K 御 ▶ K 君 ▶ K 君 ▶ ○ 君

Dark energy constraints Likelihood surfaces

• Parameter estimates from mean of marginalised distributions

•
$$
\Omega_{\Lambda} = 0.63^{+0.18}_{-0.17}
$$
; $w = -0.77^{+0.35}_{-0.36}$ using SMHW

•
$$
\Omega_{\Lambda} = 0.52^{+0.20}_{-0.20}
$$
; $w = -0.73^{+0.42}_{-0.46}$ using SBW

イロト イ団ト イヨト イヨト

 \Rightarrow

Dark energy constraints Parameter estimates

- Also considered case *w* = −1
	- $\Omega_{\Lambda}=$ 0.70 $^{+0.15}_{-0.15}$ using SMHW
	- $\Omega_{\Lambda}=$ 0.57 $^{+0.18}_{-0.18}$ using SBW
- Reject $\Omega_{\Lambda} = 0$ at $> 99\%$ significance
	- Ω_{Λ} > 0.1 at 99.9% using SMHW
	- Ω_{Λ} > 0.1 at 99.7% using SBW

4 0 8 ← nP × 2990

重

メミメメ ヨメ

Dark energy constraints Parameter estimates

- Also considered case *w* = −1
	- $\Omega_{\Lambda}=$ 0.70 $^{+0.15}_{-0.15}$ using SMHW
	- $\Omega_{\Lambda}=$ 0.57 $^{+0.18}_{-0.18}$ using SBW
- Reject $\Omega_{\Lambda} = 0$ at $> 99\%$ significance
	- Ω_{Λ} > 0.1 at 99.9% using SMHW
	- Ω_{Λ} > 0.1 at 99.7% using SBW

 290

B

重

Outline

- [Integrated Sachs-Wolfe \(ISW\) effect](#page-2-0)
	- **[Physical origin](#page-3-0)**
	- [Detecting the effect](#page-7-0) \bullet
- [The continuous spherical wavelet transform \(CSWT\)](#page-12-0)
	- [Dilations and mother wavelets on the sphere](#page-13-0) \bullet
	- **•** [Transform](#page-17-0)
- 3 [Cross-correlation in wavelet space](#page-21-0)
	- [Wavelet covariance estimator](#page-22-0)
	- [Comparison of wavelets](#page-26-0)
- 4 [Analysis procedure](#page-30-0)
- **[Results](#page-35-0)**
	- **•** [Detections](#page-36-0)
	- [Dark energy constraints](#page-45-0)

 290

→ 重 ト 4

重き G.

Summary

- Used spherical wavelets to detect ISW effect
- **Detection of ISW effect made at almost 4** σ \rightarrow effectiveness of wavelets
- Foregrounds and systematics *not* likely source of detection
- Independent evidence of dark energy
- Consistent constraints on dark energy
	- Good consistency check with direct estimates from other approaches
	- Wavelets of similar performance for constraining dark energy as other ISW techniques

K 何 ▶ K ヨ ▶ K ヨ ▶

 \Rightarrow

 QQ